# **GABRIEL TRINDADE**

Holding a bachelor's degree in Physics from the Institute of Physics of São Carlos (IFSC-USP), the student completed the master's degree at the Institute of Mathematical and Computational Sciences (ICMC-USP) in the area of differential geometry. Currently, he is a PhD candidate in Physics at the Fresnel Institute and Aix-Marseille University (AMU), working on geometric information theory and its applications in light polarization. His experience includes research in Ricci flow on surfaces, information geometry, and real hyperbolic geometry.

### CONTACT

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- in LinkedIn
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- Lattes 6409479129700945

## **LANGUAGES**

PortugueseNativeEnglishAdvancedFrenchIntermediateSpanishBasic

## **TECHNICAL SKILLS**

MathematicaVersion 14.3Python 3Version 3.9.6InkScapeVersion 1.4.2ZoteroVersion 7.0.29

LaTex

## **TOPICS OF INTEREST**

- Geometric information theory and information geometry
- Computational geometry
- · Learning on manifolds
- · Affine-invariant geometry
- Matrix information geometry
- Statistical manifolds
- Geometric statistics for light polarization
- Light polarization theory
- Real hyperbolic geometry

## **EDUCATION**

## **Bachelor in Physics**

- **2017 2021**
- University of São Paulo (USP) Institute of Physics of São Carlos - Brazil
- Final work: An introduction to Ricci flow on surfaces
- Advisor: Prof. Dr. Carlos Henrique Grossi Ferreira

## Master's degree in Mathematics

- **2**021 2023
- University of São Paulo (USP)
  Institute of Mathematics and Computer Sciences Brazil
- **Master's thesis:** From statistical models to  $\alpha$ -connections: an overview of information geometry
- Advisor: Prof. Dr. Carlos Henrique Grossi Ferreira

## Ph.D. in Physics and Materials Science

## **Specialization in Theoretical and Mathematical Physics**

- **i** 2024 present
- University of Aix-Marseille (AMU) Fresnel Institute - France
- Ph.D. project: Extrinsic statistics for complex covariance matrices and partially polarized light
- Advisors: Prof. Dr. Emmanuel Chevallier
  Prof. Dr. André Nicolet

## **Professional Course in Information Technology**

- **2014 2016**
- Paula Souza State Center for Technological Education (CEETEPS) Brazil

## PROJECTS AND RESEARCH ACTIVITIES

## Introduction to Ricci flow

- **=** 2020 2020
- University of São Paulo (USP) Institute of Physics of São Carlos - Brazil
- **① Description:** This undergraduate project focused on studying prerequisites for understanding the Ricci flow, covering results from analysis on smooth manifolds, tensor calculus, and Riemannian geometry.
- Advisor: Prof. Dr. Carlos Henrique Grossi Ferreira
- **T** Funded by Conselho Nacional de Desenvolvimento Científico e Tecnológico (CNPq)

#### An introduction to Ricci flow on surfaces

**2020 - 2021** 

University of São Paulo (USP) Institute of Physics of São Carlos - Brazil

1 Description: This project aimed to study results of the Ricci curvature flow on surfaces, focusing on those with non-positive Euler characteristic and providing qualitative insights into this flow in three dimensions

Advisor: Prof. Dr. Carlos Henrique Grossi Ferreira

funded by Fundação de Amparo à Pesquisa do Estado de São Paulo (FAPESP)

## From statistical models to $\alpha$ - connections: an overview of information geometry

**=** 2021 - 2023

University of São Paulo (USP) Institute of Mathematics and Computer Sciences - Brazil

**1 Description:** This project consisted of a presentation on the information geometry, organized as a compilation of fundamental concepts and results in the field, as well as applications in quantum information theory for the calculation of geometric quantum speed limits. Thus, statistical models were studied from Riemannian geometry. Furthermore, finite information geometry was explored, starting from an extrinsic approach and introducing the  $\alpha$ -geometry. Additionally, dualistic manifolds and statistical manifolds were investigated. and through this intrinsic approach to information geometry, flat information geometry was studied.

Advisor: Prof. Dr. Carlos Henrique Grossi Ferreira

illimitation france de la Funded by Fundação de Amparo à Pesquisa do Estado de São Paulo (FAPESP)

## Extrinsic statistics for complex covariance matrices and partially polarized light

**2024** - present

University of Aix-Marseille (AMU) Fresnel Institute - France

**1 Description:** This PhD research aims to develop new statistical tools for analyzing the polarization state of partially polarized light, represented by  $2 \times 2$ complex Hermitian matrices. Traditional Euclidean methods are inadequate as they do not respect the transformations induced by Jones matrices modeling material interactions. To address this, the study will explore non-isometric embeddings into Euclidean spaces that align with these transformations. This approach will be applied to polarization and covariance matrices - including block-Toeplitz matrices from radar signal processing - to tackle problems involving random electromagnetic wave.

Advisors: Prof. Dr. Emmanuel Chevallier Prof. Dr. André Nicolet

**1** Funded by AMU - Ministère Enseignement Supérieur

## TEACHING EXPERIENCE

### Short course taught: An introduction to information geometry

**2**023

Course load: 8 h

University of São Paulo (USP) Institute of Mathematics and Computer Sciences - Brazil

- Short course held during the Summer Program in Mathematics at ICMC-USP.
- The goal was to disseminate basic knowledge about information geometry among undergraduate students.
- The candidate produced introductory lecture notes on the topic, presents here.

## **X** AWARDS AND TITLES

Medal in the Brazilian Public School **Mathematics Olympiad** 

- 🗰 2011 Silver
- 2012 Bronze
- # 2013 Silver

Medal in the Brazilian Public School **Physics Olympiad** 

- # 2014 Bronze
- 2015 Bronze

Honorable Mention in the Brazilian Public **School Mathematics Olympiad** 

- 20142015
- **#** 2016

## **REFERENCES**

#### **Emmanuel Chevallier**

Professor at University of Aix-Marseille PhD supervisor

emmanuel.chevallier@univ-amu.fr

#### André Nicolet

Professor at University of Aix-Marseille Director of Ph.D. thesis

andre.nicolet@univ-amu.fr

### **Carlos Henrique Grossi Ferreira**

Senior researcher at NeoSpace AI Undergraduate, graduate, and master's thesis super-

grossi@icmc.usp.br

### Diogo de Oliveira Soares Pinto

Professor at University of São Paulo Undergraduate professor

dosp@ifsc.usp.br

## **COMPLEMENTARY FORMATION**

ightharpoonup 2  imes 2 matrices or split-quaternions: applied to the study of high Brazilian Mathematical Society (SBM)	yperbolic space	Course load: 4 h
ightharpoonup Generating functions and the counting of symmetric $(0,1)$ M $ ightharpoonup$ Brazilian Mathematical Society (SBM)	atrices	• Course load: 4 h
<ul> <li>➤ The differential geometry of domes: from ancient Western ar</li> <li>P Brazilian Mathematical Society (SBM)</li> </ul>		indigenous constructions  Course load: 4 h
➤ Great Moments in the History of Mathematics  ¶ University of São Paulos (USP)	<b>=</b> 2022	Course load: 15 h
➤ An Introduction to Percolation  ☐ University of São Paulos (USP)	<b>=</b> 2022	Course load: 14 h
> Real Analysis  • University of São Paulos (USP)	<b>=</b> 2021	Course load: 60 h
➤ Differential geometry of curves and surfaces in Minkowski spare.  Federal University of Paraíba (UFPB)	ace <b>ä</b> 2021	Course load: 14 h
➤ Hyperbolic geometry without coordinates  ☐ University of São Paulos (USP)	<b>=</b> 2020	Course load: 12 h
➤ Linear structures in geometry  ☐ University of São Paulos (USP)	<b>=</b> 2019	Course load: 12 h
➤ Solution of the LSM for a (seemingly) insolvable problem  • University of São Paulos (USP)	<b>=</b> 2019	Course load: 6 h
> Introduction to general relativity Pederal University of São Carlos (UFSCar)	<b>=</b> 2018	Course load: 4 h
➤ Junior Scientific Initiation Program  ■ Brazilian Olympiad of Public School Mathematics (OBMEP)	<b>=</b> 2013	Course load: 80 h
➤ Junior Scientific Initiation Program  ■ Brazilian Olympiad of Public School Mathematics (OBMEP)	<b>=</b> 2012	Course load: 80 h
<b>EVENTS</b>		
<ul> <li>&gt; 7th International Conference on Geometric Science of Inform</li> <li>➡ Oral presentation: Fast equivariant k-means on SPD matrice</li> <li>➡ 2025</li> <li>➡ Type: Congress</li> </ul>		
> 35th Brazilian Mathematical Colloquium	Rio de Janeiro - E	Brazil
> Fête de la Science  Outreach presentation: La lumière et ses applications  Type: Outreach event	¶ Marseille - France	e
> XXVIII Brazilian School of Probability  == 2025	Belo Horizonte -	Brazil
> XI Biennial of Mathematics  == 2024	🖣 São Carlos - Brazi	il

XXI School of Dif	ferential Geometry	
<b>=</b> 2024	••• Type: Congress	🕈 Diamantina - Brazil
> XXVII Brazilian S	chool of Probability	
🔐 Poster presenta	tion: Information geometry: when statis	stics meets geometry
<b>=</b> 2024	••• Type: Congress	P Salvador - Brazil
> Geometry in Alg	ebra and Algebra in Geometry VII	
🔐 Poster presenta	tion: An overview of finite information ${\mathfrak g}$	geometry
<b>=</b> 2023	••• Type: Congress	P Belo Horizonte - Brazil
> Workshop on Alg	gebraic Topology and Applications	
<b>2</b> 023	••• Type: Workshop	🕈 São Carlos - Brazil
> XXIII Symposium	on Mathematics for Undergraduate St	udents
🔐 Poster presenta	tion: Introduction to Ricci flow	
<b>2</b> 020	••• Type: Symposium	🕈 São Carlos - Brazil
> 10th Integrated V	Veek of Undergraduate and Graduate S	tudies at the São Carlos Institute of Physics
Poster presenta	ation: An introduction to Ricci flow on su	urfaces
Member of the	organizing committee	
<b>=</b> 2020	••• Type: Symposium	P São Carlos - Brazil

## **66** PUBLICATIONS

Fast Equivariant K-Means on SPD Matrices Using Log-Extrinsic Means

**Trindade**, **G**., Chevallier, E., Nicolet, A., Nielsen, F. (2025, October). Fast Equivariant K-Means on SPD Matrices Using Log-Extrinsic Means. In International Conference on Geometric Science of Information (pp. 263-270). Cham: Springer Nature Switzerland.

**=** 2025

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